## Ma

KEY STAGE

# Mathematics mark schemes <br> Paper 1 and Paper 2 

## National Curriculum assessments

## [BLANK PAGE]

This page is intentionally blank.

## Introduction

The Standards and Testing Agency (STA) is responsible for the development and delivery of statutory tests and assessments in 2013. The STA is an executive agency of the Department for Education. The test papers will be marked by external markers employed by STA.

This booklet contains the mark schemes for level 6 mathematics paper 1 and paper 2. Level threshold tables will be available at www.education.gov.uk/ks2 from Tuesday 9 July 2013.

Paper 1 carries a total of 26 marks. Paper 2 carries a total of 24 marks. There is no mental mathematics test in the level 6 test.

The mark schemes were written alongside the questions, with children's responses added as examples to the mark schemes following trials. The mark schemes indicate the criteria on which judgements should be made. In areas of uncertainty, however, markers should use professional judgement based on the training they have received.

A number of questions in both papers contain elements of using and applying mathematics. These are not referenced explicitly in the mark scheme.

The 2013 Key Stage 2 level 6 mathematics tests and mark schemes were produced by the Key Stage 2 mathematics test development team at STA.

## General guidance

The marking information for each question is set out in the form of tables, which start on page 10 of this booklet.

The 'Question' column on the left-hand side of each table provides a quick reference to the question number and the question part.

The 'Requirement' column may include two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working; and
- examples of some different types of correct response.

The 'Mark' column indicates the total number of marks available for each question part.
The 'Additional guidance’ column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as the range of acceptable answers, is provided as necessary. The '!' is used to indicate responses that are not presented conventionally but are awarded mark(s) in recognition of children's mathematical understanding at this age.

## Applying the mark schemes

To ensure consistency of marking, the most frequent queries about applying the mark scheme are listed on pages 4 and 5 along with the action the marker will take. This is followed by further guidance on pages 6 and 7 relating to the marking of questions that involve money, time and other measures. Specific guidance on marking responses involving coordinates, probability and algebra is given on pages 8 and 9 . Unless otherwise specified in the mark scheme, markers will apply these guidelines in all cases.

## What if...

The child's response is numerically or algebraically equivalent to the answer in the mark scheme.

The child's response does not match closely any of the examples given.

The child has responded in a non-standard way.

There appears to be a misreading affecting the working.

No answer is given in the expected place, but the correct answer is given elsewhere.

The child's answer is correct but the wrong working is shown.

The response in the answer box is wrong but the correct answer is shown in the working.

## Marking procedure

Markers will award the mark unless the mark scheme states otherwise.

Markers will use their judgement in deciding whether the response corresponds with the statement of the requirements given in the 'Requirement' column. Reference will also be made to the 'Additional guidance' column and, if there is still uncertainty, markers will contact the supervising marker.

Calculations, formulae and written responses do not have to be set out in any particular format. Children may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, will be accepted.

This is when the child misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, one mark only will be deducted.

Where a child has shown understanding of the question, the mark(s) will be given. In particular, where a word or number response is expected, a child may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.

A correct response will always be marked as correct.

Where appropriate, detailed guidance will be given in the mark scheme, which markers will follow. If no guidance is given, markers will examine each case to decide whether:

- the incorrect answer is due to a transcription error
- the child has continued to give redundant extra working which does not contradict work already done
- the child has continued to give redundant extra working which does contradict work already done.

If so, the mark will be awarded.

If so, the mark will be awarded.

If so, the mark will not be awarded.

What if...
The correct response has been
crossed out and not replaced.

More than one answer is given.

The answer is correct but, in a later part of the question, the child has contradicted this response.

The child has drawn lines which do not meet at the correct point.

## Marking procedure

Any legible crossed-out work that has not been replaced will be marked according to the mark scheme. If the work is replaced, then crossed-out work will not be considered.

If all answers are correct (or a range of answers is given, all of which are correct), the mark will be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark will be awarded.

A mark given for one part will not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.

Markers will interpret the phrase 'slight inaccuracies in drawing' to mean 'within or on a circle of radius 2 mm with its centre at the correct point'.


## Recording marks awarded

Marking will take place on screen with markers viewing scanned images of children's scripts. Marks should be input on screen in accordance with the guidance given on the use of the on-screen marking software.

For multiple mark questions, markers will record the award of $3,2,1$ or 0 as appropriate according to the mark scheme criteria. There will be provision in the software to record questions not attempted (NR: no response).

The software will aggregate mark totals automatically.
Further details on recording of marks and the use of the on-screen system will be given at marker training.

## Marking specific types of question - summary of additional guidance

## Responses involving money



## Responses involving time

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| A time interval for example: 2 hours 30 minutes | 2 hours 30 minutes <br> Any unambiguous, correct indication, eg: <br> $2 \frac{1}{2}$ hours <br> 2.5 hours <br> 2h 30 <br> 2h 30 min <br> 230 <br> 150 minutes <br> 150 <br> Digital electronic time, ie: <br> 2:30 | Incorrect or ambiguous time interval, eg: <br> 2.30 <br> 2-30 <br> 2,30 <br> 230 <br> 2.3 <br> 2.3 hours <br> 2.3h <br> 2h 3 <br> 2.30 min |
| A specific time for example: 8:40am, 17:20 | 8:40am <br> 8:40 <br> twenty to nine <br> Any unambiguous, correct indication, eg: <br> 08.40 <br> 8.40 <br> 0840 <br> 840 <br> 8-40 <br> 8,40 <br> Unambiguous change to 12 - or 24-hour clock, eg: <br> 17:20 as $5: 20 \mathrm{pm}$ or $17: 20 \mathrm{pm}$ | Incorrect time, eg: <br> 8.4am <br> 8.40pm <br> Incorrect placement of separators, spaces, etc or incorrect use or omission of 0 , eg: <br> 840 <br> 8:4:0 <br> 8.4 <br> 084 |

## Responses involving measures

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| Where units are given (eg: kg, m, l) <br> for example: 8.6 kg | 8.6 kg |  |
|  | Any unambiguous indication of the correct measurement, eg: | Incorrect or ambiguous use of units, eg: 8600kg |
| kg | 8.60 kg |  |
|  | 8.6000 kg |  |
|  | $8 \mathrm{~kg} \mathrm{600g}$ |  |

## Responses involving coordinates

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| Responses involving coordinates <br> for example: $(5,7)$ | Unconventional notation, eg: $(05,07)$ <br> (five, seven) $\begin{aligned} & x y \\ & (5,7) \\ & (x=5, y=7) \end{aligned}$ | Incorrect or ambiguous notation, eg: $\begin{aligned} & (7,5) \\ & y x \\ & (7,5) \\ & (5 x, 7 y) \\ & \left(5^{x}, 7^{y}\right) \\ & (x-5, y-7) \end{aligned}$ |

## Responses involving probability

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| A numerical probability should be expressed as a decimal, fraction or percentage only for example: $0.7 \quad \frac{7}{10} \quad 70 \%$ | Equivalent decimals, fractions and percentages, eg: <br> 0.700 $\frac{70}{100}$ $\frac{35}{50}$ $70.0 \%$ <br> A probability correctly expressed in one acceptable form, which is then incorrectly converted but is still less than 1 and greater than 0 , eg: $\frac{70}{100}=\frac{18}{25}$ | The first four categories of error below should be ignored if accompanied by an acceptable response, but should not be accepted on their own. <br> However, to avoid penalising the first three types of error below more than once within each question, do not award the mark for the first occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld. <br> ! A probability that is incorrectly expressed, eg: <br> 7 in 10 <br> 7 over 10 <br> 7 out of 10 <br> 7 from 10 <br> ! A fraction with non-integers in the numerator and/or denominator. <br> ! A probability expressed as a percentage without a percentage sign. <br> ! A probability expressed as a ratio, eg: $7: 10,7: 3,7$ to 10 <br> A probability greater than 1 or less than 0 |

## Responses involving algebra



## Note

If a child leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed above.

If a child changes the unit given in the answer box, then their answer must be equivalent to the correct answer using the unit they have chosen, unless otherwise indicated in the mark scheme.

## 102013 Key Stage 2 level 6 mathematics tests mark schemes

## Paper 1: Calculator not allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 1 | Gives a correct probability, eg: <br> - $45 \%$ <br> - 0.45 <br> - $\frac{45}{100}$ <br> - $\frac{9}{20}$ <br> Shows or implies a complete correct method, with not more than one computational error, eg: <br> - $\frac{1}{4}=100 \div 4=40 \%$ (error) $40 \%+30 \%=70 \%$ $100 \%-70 \%=30 \%$ <br> - $\frac{1}{4}=\frac{4}{20}$ (error) $\begin{aligned} & 30 \%=\frac{6}{20} \\ & \frac{4}{20}+\frac{6}{20}=\frac{10}{20} \\ & 1-\frac{10}{20}=\frac{10}{20} \end{aligned}$ <br> - $1-\frac{1}{4}-30 \%$ <br> $1-0.25-0.30=0.55$ (error) <br> - $P($ Salt \& Vin $)=1-P($ Prawn $)-P($ Cheese $)$ 100\%-25\%-30\% | $2 m$ <br> or <br> 1m | ! Probability <br> See guidance (page 8) <br> ! Probability expressed as a percentage without a percentage sign <br> Condone for 1 m , ie: <br> - 45 <br> ! Conversion between fractions, decimals and percentages <br> Within a complete correct method, conversions must be correct and/or show the method of conversion <br> $x$ Incomplete methods which do not convert the probabilities to a common format, eg: <br> - $1-\frac{1}{4}-30 \%$ |
| 2 | Gives the three correct numbers in their correct positions, ie: <br> Gives two correct numbers in their correct positions | $2 m$ <br> or <br> 1 m | Unambiguous indication <br> Equivalent fractions, eg: <br> - $7 \frac{5}{10}$ for 7.5 |
| 3 | Completes all three rows correctly, eg: <br> Completes two rows correctly | 2m <br> or <br> 1 m | ! Measures <br> See guidance (page 7) <br> $\checkmark$ Side lengths in each row may be given in any order <br> $\checkmark$ Accept correct values with cm omitted eg, for the rectangle: <br> - 15315 |

## Paper 1: Calculator not allowed

| Question | Requirement | Mark | Additional guidance |  |
| :---: | :---: | :---: | :---: | :---: |
| 4a | 50 | 1 m |  |  |
| 4b | 5 | 1 m |  |  |
| 5a | $\frac{1}{20}$ or equivalent | 1 m | Equivalent fractions, decimals or percentages, eg: <br> - $5 \%$ <br> - 0.05 <br> - $\frac{5}{100}$ <br> $x 5$ without a percentage sign |  |
| 5b | 95 | 1 m | $x$ | Equivalent fractions or decimals |
| 6 a | 302 | 1 m |  |  |
| 6b | 49 | 2 m | ! Correct embedded solutions <br> Award 1 m for a response which shows 49 as the embedded solution to their working |  |
|  | Shows or implies a correct first step of algebraic manipulation that either reduces the number of terms or collects variables on one side of the equation and numbers on the other, eg: <br> - $2 s=100-2$ <br> - $s=98 \div 2$ <br> OR <br> Shows or implies a complete correct method, eg: <br> - $(100-2) \div 2$ | 1 m |  |  |
| 7 | $\frac{3}{10}$ or equivalent | $2 m$ or | $\checkmark$ | Equivalent fractions, decimals or percentages |
|  | Shows or implies a complete correct method and no conceptual errors, eg: <br> - Shaded fraction is $\frac{1}{5}+\frac{1}{5}=\frac{2}{5}$ Fraction of total white area $=1-\frac{2}{5}=\frac{3}{5}$ $\frac{3}{5} \div 2$ <br> - $\frac{1}{5}+\frac{1}{5}=20 \%+20 \%=30 \%$ (error) <br> White area $=70 \%$ <br> Each white area $=35 \%$ | 1 m | $!$ | 30 with no \% sign <br> Accept for 1 m as evidence of a correct method $\frac{1.5}{5} \text { or } \frac{1 \frac{1}{2}}{5}$ <br> Accept for 1 m as evidence of a correct method (incorrect notation for $\frac{3}{5} \div 2$ ) |

## 122013 Key Stage 2 level 6 mathematics tests mark schemes

## Paper 1: Calculator not allowed

## Question

8

Requirement
Indicates No and gives a correct explanation that includes indicating two different areas, eg:

- A rectangle with sides 6 cm by 2 cm has a perimeter of 16 cm and an area of $12 \mathrm{~cm}^{2}$ but a rectangle with sides 5 cm and 3 cm has the same perimeter of 16 cm but it has an area of $15 \mathrm{~cm}^{2}$ which is different so she is not correct
- A square with sides 3 cm by 3 cm and a rectangle with sides 4 cm by 2 cm have the same perimeter of 12 cm but they have different areas of $9 \mathrm{~cm}^{2}$ and $8 \mathrm{~cm}^{2}$


## Mark

1m

Additional guidance
$\checkmark$ Minimally acceptable explanation, eg:

- $6 \times 2=12,5 \times 3=15$

! Ignore any incorrect units given in an otherwise correct explanation, eg:
- $6^{2}$ for $6 \mathrm{~cm}^{2}$
! Indicates Yes, or no decision made, but explanation clearly correct

Condone, provided the explanation is more than minimal
$x$ Incomplete or incorrect explanation, eg:

- $6 \times 2,5 \times 3$
- Two rectangles, one with sides 6 cm by 5 cm and one with sides 8 cm by 3 cm have the same perimeter of 22 cm but they don't have the same area


7


8

## Paper 1: Calculator not allowed



## Paper 1: Calculator not allowed



## Paper 1: Calculator not allowed



## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 1 | Makes all four correct decisions, ie: <br> Makes three correct decisions | $2 m$ <br> or <br> $1 m$ | $\checkmark$ Accept unambiguous indications, eg: <br> - ' $y$ ' or ' $x$ ' for ticked in each row |
| 2 | $525$ <br> 175 seen (the weight of the elephant) <br> OR <br> Shows or implies a complete correct method, eg: <br> - $\frac{700}{4}=170$ (error) <br> $170 \times 3$ | $2 m$ <br> or <br> $1 m$ | ! Measures <br> See guidance (page 7) |
| 3 | $73^{\circ}$ seen (one of the other angles in the isosceles triangle) <br> OR <br> Shows or implies a complete correct method, eg: <br> - $180-34=144$ (error) $\begin{aligned} & 144 \div 2=72 \\ & 90-72=28 \text { (error) } \end{aligned}$ | $2 m$ <br> or <br> 1 m | ! Answer written on diagram <br> Accept providing there is no ambiguity |
| 4 | Identifies all three graphs correctly, ie: <br> - Chen A Megan C Alfie B | 1 m | $\checkmark$ Unambiguous indications of the correct graph for each person, eg: <br> - Names written on scatter graphs |

## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :--- | :--- | :--- | :--- | :--- |
| 5 | Gives only the three correct prime numbers in any <br> order, ie: <br> - $37,41,43$ | $\mathbf{2 m}$ |  |

## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 8 | 64 <br> Shows the value 19200 (volume of the tank) <br> OR <br> Shows or implies a complete correct method, eg: <br> - $(40 \times 40 \times 12) \div 300=58$ (error) | 2m <br> or <br> $1 m$ | ! For 2m, condone 63.99(...) (some calculator displays will show this as their final answer) <br> ! For 1m, condone 63.9 as evidence of an appropriate method (calculator display incorrectly rounded) |
| 9 | 2.2 <br> 10.648 or 10.65 or 10.6 seen <br> (the answer to $2.2 \times 2.2 \times 2.2$ ) <br> OR <br> 2.15(...) seen <br> OR <br> Shows a correct method using trial and improvement, eg: <br> - $2 \times 2 \times 2=8$ $\begin{aligned} & 2.5 \times 2.5 \times 2.5=15.625 \\ & 2.1 \times 2.1 \times 2.1=9.261 \end{aligned}$ <br> - 2.4 because it's bigger than 2.1 which was too small, but smaller than 2.5 which was too big | $2 m$ <br> or <br> 1m | ! For 1m, accept 2.1 (correct value but not correctly rounded) <br> ! Trial and improvement methods <br> There must be at least three trials. At least three of these trials must reduce the interval in which the solution is known to lie and at least two trials must use values to 1 decimal place <br> ! Numbers not evaluated within trial and improvement methods <br> Condone methods that do not show evidence of evaluating the final number, eg: <br> - 2.3 because I know it's between 2 and 2.5 |

## Paper 2: Calculator allowed

$\left.\begin{array}{|l|l|l|l|l|}\hline \text { Question } & \text { Requirement } & \text { Mark } & \text { Additional guidance } \\ \hline \mathbf{1 0} & 2 & \mathbf{2 m} & \text { ! } & \text { Money } \\ \text { See guidance (page 6) }\end{array}\right]$

## Standards <br> \& Testing <br> Agency

2013 Key Stage 2 level 6 mathematics: Mark schemes
Print version product code: STA/13/6038/p ISBN: 978-1-4459-5761-6
Electronic PDF version product code: STA/13/6038/e ISBN: 978-1-4459-5762-3
© Queen's Printer and Controller of HMSO 2013
Material contained in these booklets may be reproduced for educational and training purposes within a school setting, provided you acknowledge the copyright ownership of the material and you give the title of the source document. Reproduction or re-use of the material is not permitted for any commercial purpose.

## For more copies

Additional printed copies of this mark scheme are not available. It can be downloaded from STA's orderline at http://orderline.education.gov.uk.

