## Ma

KEY STAGE

# Mathematics mark schemes <br> Paper 1 and paper 2 

## National curriculum assessments

22014 key stage 2 level 6 mathematics tests mark schemes

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## Introduction

The Standards and Testing Agency (STA) is responsible for the development and delivery of statutory tests and assessments. The STA is an executive agency of the Department for Education (DfE).

This booklet contains the mark schemes for the assessment of level 6 mathematics. Level threshold tables will be available at www.education.gov.uk/ks2 from Tuesday 8 July, 2014.

The level 6 mathematics test is made up of two papers and contains a total of 50 marks.
Paper 1: non-calculator paper (26 marks)
Paper 2: calculator paper (24 marks)
There is no mental mathematics paper in the level 6 test.
As in previous years, external markers will mark the key stage 2 national curriculum tests. The mark schemes are made available to teachers after the tests have been taken.

The mark schemes were written and developed alongside the questions. Children's responses from trialling have been added as examples to the mark schemes to ensure they reflect how children respond to the questions. The mark schemes indicate the criteria on which judgements should be made. In applying these principles, markers use professional judgement based on the training they have received.

A number of questions in both papers contain elements of using and applying mathematics. These are not referenced explicitly in the mark scheme.

## The mathematics test mark schemes

The marking information for each question is set out in the form of tables, which start on page 10 of this booklet.

The 'Question' column on the left-hand side of each table provides a quick reference to the question number and the question part.

The 'Requirement' column may include two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working; and
- examples of some different types of correct response.

The 'Mark' column indicates the total number of marks available for each question part.
The 'Additional guidance' column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as the range of acceptable answers, is provided as necessary. The '!' is used to indicate responses that are not presented conventionally but are awarded one or more marks in recognition of children's mathematical understanding at this age.

## Applying the mark schemes

To ensure consistency of marking, the most frequent queries about applying the mark schemes are listed on pages 4 and 5 along with the action the marker will take. This is followed by further guidance on pages 6 and 7 relating to the marking of questions that involve money, time and other measures. Specific guidance on marking responses involving coordinates, probability and algebra is given on pages 8 and 9 . Unless otherwise specified in the mark schemes, markers will apply these guidelines in all cases.

## General guidance in marking the level 6 mathematics tests

## What if...

The child's response is numerically or algebraically equivalent to the answer in the mark scheme.

The child's response does not match closely any of the examples given.

The child has responded in a non-standard way.

There appears to be a misreading affecting the working.

No answer is given in the expected place, but the correct answer is given elsewhere.

The child's answer is correct, but the wrong working is shown.

The response in the answer box is wrong, but the correct answer is shown in the working.

## Marking procedure

Markers will award the mark unless the mark scheme states otherwise.

Markers will use their judgement in deciding whether the response corresponds with the statement of the requirements given in the 'Requirement' column. Reference will also be made to the 'Additional guidance' column and, if there is still uncertainty, markers will contact the supervising marker.

Calculations, formulae and written responses do not have to be set out in any particular format. Children may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, will be accepted.

This is when the child misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, one mark only will be deducted.

Where a child has shown understanding of the question, the mark(s) will be given. In particular, where a word or number response is expected, a child may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.

A correct response will always be marked as correct.

Where appropriate, detailed guidance will be given in the mark schemes, which markers will follow. If no guidance is given, markers will examine each case to decide whether:

- the incorrect answer is due to a transcription error
- the child has continued to give redundant extra working which does not contradict work already done
- the child has continued to give redundant extra working which does contradict work already done.

If so, the mark will be awarded.

If so, the mark will be awarded.

If so, the mark will not be awarded.

## What if...

The correct response has been crossed out and not replaced.

More than one answer is given.

The answer is correct but, in a later part of the question, the child has contradicted this response.

The child has drawn lines which do not meet at the correct point.

## Marking procedure

Any legible crossed-out work that has not been replaced will be marked according to the mark scheme. If the work is replaced, then crossed-out work will not be considered.

If all answers are correct (or a range of answers is given, all of which are correct), the mark will be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark will be awarded.

A mark given for one part will not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.

Markers will interpret the phrase 'slight inaccuracies in drawing' to mean 'within or on a circle of radius 2 mm with its centre at the correct point'.


## Recording marks awarded

Marking will take place on screen with markers viewing scanned images of children's scripts. Marks should be input on screen in accordance with the guidance given on the use of the on-screen marking software.

For multiple-mark questions, markers will record the award of $3,2,1$ or 0 as appropriate, according to the mark-scheme criteria. There will be provision in the software to record questions not attempted (N/A: not attempted).

The software will aggregate mark totals automatically.
Further details on recording marks and the use of the on-screen system will be given at marker training.

## Marking specific types of question: summary of additional guidance

## Responses involving money



## Responses involving time

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| A time interval for example: 2 hours 30 minutes | 2 hours 30 minutes <br> Any unambiguous, correct indication, eg: <br> $2 \frac{1}{2}$ hours <br> 2.5 hours <br> 2h 30 <br> 2h 30 min <br> 230 <br> 150 minutes <br> 150 <br> Digital electronic time, ie: <br> 2:30 | Incorrect or ambiguous time interval, eg: <br> 2.30 <br> 2-30 <br> 2,30 <br> 230 <br> 2.3 <br> 2.3 hours <br> 2.3h <br> 2h 3 <br> 2.30 min |
| A specific time for example: 8:40am, 17:20 | 8:40am <br> 8:40 <br> twenty to nine <br> Any unambiguous, correct indication, eg: <br> 08.40 <br> 8.40 <br> 0840 <br> 840 <br> 8-40 <br> 8,40 <br> Unambiguous change to 12 - or 24-hour clock, eg: <br> 17:20 as $5: 20 \mathrm{pm}$ or $17: 20 \mathrm{pm}$ | Incorrect time, eg: <br> 8.4am <br> 8.40pm <br> Incorrect placement of separators, spaces etc or incorrect use or omission of 0 , eg: <br> 840 <br> 8:4:0 <br> 8.4 <br> 084 |

## Responses involving measures

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| Where units are given (eg: kg, m, l) <br> for example: 8.6 kg | 8.6 kg |  |
|  | Any unambiguous indication of the correct measurement, eg: | Incorrect or ambiguous use of units, eg: 8600 kg |
| kg | 8.60 kg |  |
|  | 8.6000 kg |  |
|  | $8 \mathrm{~kg} \mathrm{600g}$ |  |

## Responses involving coordinates

|  | Accept | Do not accept |
| :--- | :--- | :--- |
| Responses involving <br> coordinates | Unconventional notation, eg: | Incorrect or ambiguous notation, eg: |
| for example: | $(05,07)$ | $(7,5)$ |
| $(5,7)$ | (five, seven) | $y x$ |
|  | $x y$ | $(7,5)$ |
|  | $(5,7)$ | $(5 x, 7 y)$ |
|  | $(x=5, y=7)$ | $\left(5^{x}, 7^{y}\right)$ |
|  |  | $(x-5, y-7)$ |

## Responses involving probability

|  | Accept | Do not accept |
| :---: | :---: | :---: |
| A numerical probability should be expressed as a decimal, fraction or percentage only for example: $0.7 \quad \frac{7}{10} \quad 70 \%$ | Equivalent decimals, fractions and percentages, eg: <br> 0.7000 $\begin{aligned} & \frac{70}{100} \\ & \frac{35}{50} \\ & 70.0 \% \end{aligned}$ <br> A probability correctly expressed in one acceptable form, which is then incorrectly converted or incorrectly expressed, but is less than one and greater than zero, eg: $\frac{70}{100}=\frac{18}{25}$ $\frac{70}{100}=7 \%$ $\frac{70}{100} \text { is } 7: 10$ | The following categories should not be credited if given as the final answer to a question. However, in a multiple-mark question, sight of these can be awarded partial credit in an otherwise correct method. <br> ! Probability that is incorrectly expressed, eg: <br> 7 in 10 <br> 7 over 10 <br> 7 out of 10 <br> 7 from 10 <br> ! Fraction with non-integers in the numerator and/or denominator. <br> ! Probability expressed as a percentage without a percentage sign. <br> ! Probability expressed as a ratio, eg: <br> $7: 10,7: 3,7$ to 10 <br> In a multiple-part question, do not award the mark for the first occurrence of each category if unaccompanied by an acceptable response; award the mark for subsequent occurrences. |

## Responses involving algebra



## Note

If a child leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed in the general guidance section (pages 4-9).

If a child changes the unit given in the answer box, then their answer must be equivalent to the correct answer using the unit they have chosen, unless otherwise indicated in the mark scheme.

## Paper 1: Calculator not allowed



## Paper 1: Calculator not allowed

| Question | Requirement |
| :--- | :--- |
| 3a | 3 |
| 3b | Gives an explanation that justifies why the range <br> cannot be 2, eg: <br> - The difference between the smallest and the <br> largest would be 2 but here it is 3 even before <br> you put any number in <br> - It must be at least 3 because $4-1=3$ <br> - The range is already 3 <br> - The range is at least the difference between <br> 1 and 4. So the range is more than 2 |

## Mark

 1mAdditional guidance
$\checkmark$ Minimally acceptable explanation
(1) Includes the following: range or 4-1 or highest - lowest and
is 3 or greater than 2, eg:

- The range is 3
- $4-1=3$

OR
(2) Shows one of the given numbers as the smallest / largest number
and
shows how the number at either end of the range should change to make range 2 , eg:

- The highest would need to be 3 , but 4 is the highest
- The lowest would need to be 2, but 1 is the lowest
- Because the highest is 4 , the lowest would need to be 2
$x$ Incomplete or ambiguous explanation, eg:
- It must be bigger than 2
- Lowest is 1 , highest 4
- Range is difference between highest and lowest
- The range is already too great between 1 and 4
! Condone responses that assume 1 is always the lowest possible number, provided the remainder of the explanation is correct
! Condone creditworthy explanations that indicate the blank card is the child's value from part (a)


## Paper 1: Calculator not allowed

| Question | Requirement |
| :--- | :--- |
| 4a | Gives a correct interpretation of the graph, eg: <br> - It is a straight line <br> - It goes up steadily <br> - The angle of the line stays the same <br> - The gradient of the line is constant |

## Mark

1m
+

## Additional guidance

$\checkmark$ Minimally acceptable explanation, eg:

- It is straight
- It doesn't bend
- It is a diagonal
$x$ Incomplete or ambiguous explanations
that do not sufficiently imply a constant speed and / or do not demonstrate the relationship holds for the entire graph, eg:
- The line goes straight up
- It is not wobbly
- It is level
- Every 5 mins he walks the same distance
- He walks 1 km in the first 15 mins and 1 km in the second 15 mins
! Values read from graph
Accept, provided it is clear the relationship holds for the entire graph.
Values should be accurate within $+/-0.1 \mathrm{~km}$ and / or +/- 2 minutes, eg:
- 0.7 km every 10 minutes
- Every 7.5 minutes he walks about half a km
! Calculation of kilometres per hour
Accept values in the range 3.7 to 4.3 km per hour inclusive.
! Accept values between 08:09 and 08:11 inclusive
! Time
See guidance (page 7)


## Paper 1: Calculator not allowed



## Paper 1: Calculator not allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 7 | $r=150 \text { and } t=110$ | 2 m | Values must be unambiguously associated with the correct letter for the award of $2 m$ or $1 m$ |
|  |  | or |  |
|  | $r$ or $t$ correct <br> OR | 1 m | ! Answers for $r$ and $t$ transposed <br> If $r$ is 110 and $t$ is 150 , then award 1 m |
|  | Shows or implies a complete, correct method for both angles, eg: |  | ! Follow-through from incorrect base angle seen on the diagram |
|  | $\begin{aligned} & \text { - } 40+50+50=180 \text { (error) } \\ & 360-50-50-50=210 \\ & 180-50=130 \end{aligned}$ |  | Award 1 m if both $r$ and $t$ correctly follow through from an incorrect angle seen at base of an isosceles triangle, eg: |
|  |  |  |  |
|  |  |  | $\begin{aligned} & r=360-180=180 \\ & t=180-60=120 \end{aligned}$ |
| 8a | Gives a pair of numbers to make the calculation correct, eg: $\square$ <br> $\frac{1}{2}+\frac{\mathbf{1}}{5}$ <br> $\frac{1}{10}+\frac{3}{5}$ | 1 m | Accept the following |
|  |  |  | $x$ Use of non-integers, eg: $\cdot \frac{1}{3.33 \ldots}+\frac{2}{5}$ |
| 8b | Gives a different pair of numbers to make the calculation correct | 1 m |  |
| 9 | 8 faces and 12 edges | 1 m |  |
| 10 | 2.5 | 1 m | $\checkmark$ Equivalent fractions or decimals |
| 11 | $12$ | $2 m$ or |  |
|  | Shows or implies a complete correct method, eg: <br> - $4 \times 6 \div 2=13$ (error) <br> - $60-(10 \times 6 \div 2)-(6 \times 6 \div 2)$ <br> - 60-48 | 1 m |  |

## Paper 1: Calculator not allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 12 | 54 seen (angle for mushroom soup) <br> OR <br> Shows or implies a correct method for tomato soup with not more than one computational error, eg: <br> - $360-90=240$ (error) $240 \div 5=48$ $48 \times 4=192$ <br> - $0.6 \times 360$ <br> - $25 \%=$ chicken <br> $75 \% \div 5=15 \%$ <br> $15 \%$ of $360^{\circ}=54^{\circ}$ <br> $54^{\circ} \times 4$ | 3m <br> or <br> 2m |  |
|  | Shows the angle representing tomato soup and mushroom soup is 270 <br> OR <br> $60 \%$ or $\frac{3}{5}$ seen (as evidence of a correct method for tomato soup) <br> OR <br> Shows or implies a correct method for finding the angle required to represent mushroom soup, eg: <br> - $360^{\circ}-90^{\circ}=260^{\circ}$ (error) <br> $260^{\circ} \div 5=40^{\circ}$ (error) <br> OR <br> Shows or implies a correct method for tomato soup with more than one computational error, eg: <br> - $360^{\circ}-90^{\circ}=240^{\circ}$ (error) <br> $240^{\circ} \times 4 \div 5=200^{\circ}$ (error) | $\begin{aligned} & \text { or } \\ & 1 \mathrm{~m} \end{aligned}$ | $x$ Tomato soup is $270^{\circ}$ <br> $x$ Methods involving drawings of pie charts, without any values given <br> $\checkmark$ Accept equivalent fractions or decimals, eg: <br> - $\frac{6}{10}$ <br> - 0.6 <br> $x$ Do not accept 60 or $60^{\circ}$ for $\mathbf{6 0 \%}$ |
| 13a | $\mathrm{P} \text { is }(-12,-30)$ | 1 m | ! Coordinates <br> See guidance (page 8) <br> $\checkmark$ Unambiguous answers written on the diagram |
| 13b | Q is $(38,-30)$ | 1 m | ! Answers for P and Q transposed <br> Award 1 mark for Q only, ie: <br> - $P$ is $(38,-30)$ <br> $Q$ is $(-12,-30)$ <br> ! Answer for Q correctly follows through from an incorrect answer for $P$ <br> Award 1 m for Q for follow-through from P as ('their $x$ ' +50 , 'their $y$ ') |

## Paper 2: Calculator allowed



## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 6a | $5.50$ | 2 m | ! Money <br> See guidance (page 6) <br> $x$ For $2 m$ and 1m, do not accept misreads of numbers given as words, eg: <br> - four instead of five |
|  | 22 seen <br> OR <br> Shows or implies a complete, correct method, eg: <br> - $\begin{aligned} c= & £ 4.50+£ 3.50 \times 5 \\ & =£ 4.50+£ 17.50=£ 21 \text { (error) } \\ & £ 21 \div 4 \end{aligned}$ | or $1 \mathrm{~m}$ | ! For 1m, accept answers with incorrect or ambiguous units as evidence of a correct method, eg: <br> - £550 <br> - £550p <br> - $£ 5.5$ <br> ! Correct embedded solutions <br> For 1 m , condone a response which shows $£ 5.50$ embedded irrespective of how it is obtained <br> $x$ Incomplete methods, eg: <br> - $3.50 \times 5=17.50$ <br> - $14.50 \div 4=3.63$ |
| 6b | 3 | 1 m |  |
| 7a 7b | $\begin{aligned} & 36 \\ & 46 \end{aligned}$ | $\begin{aligned} & 1 \mathrm{~m} \\ & 1 \mathrm{~m} \end{aligned}$ | $x$ Equivalent fractions or decimals <br> $x$ Equivalent fractions or decimals |
| 8 | Gives a correct explanation that converts the given fractions to decimals or fractions with a common denominator / numerator or percentages, eg: <br> - $\frac{4}{7}=\frac{36}{63}$ but $\frac{5}{9}=\frac{35}{63}$ <br> - $0.57142 \ldots>0.55555$ <br> - Because there is a $\frac{1}{63}$ difference between the two | 1 m | For $\frac{4}{7}$ accept: <br> - $0.57(. .$.$) or 57(. . . . \%)$ <br> For $\frac{5}{9}$ accept: <br> - 0.56 or $0.55(\ldots)$ or $56(\%)$ or $55(. . . . \%)$ <br> Minimally acceptable explanations, eg: <br> - $\frac{36}{63} \quad \frac{35}{63}$ <br> - 0.560 .57 <br> $x$ Incomplete explanations that fail to convert both fractions to a common format, eg: <br> - $\frac{4}{7}$ is 0.57 so it is bigger <br> - 9ths are smaller than 7ths and there is only one more 9th than 7 th so $\frac{4}{7}$ is greater <br> ! Condone method of conversion incorrectly expressed in an otherwise correct explanation, eg: <br> - $\frac{4}{7} \times 9=\frac{36}{63}$ |

## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 9 | Gives two numbers which differ by 1 , the lower of which is in the range 2.5 to 2.5823 exclusive, eg: <br> - 2.55 and 3.55 <br> Gives at least one number in the range <br> 2.5 to 2.5823 exclusive <br> or <br> 3.5 to 3.5823 exclusive | 2m <br> or $1 \mathrm{~m}$ | $\checkmark$ Numbers may be given in either order |
| 10 | 160 seen (the total children in the school) <br> OR <br> Shows or implies a complete, correct method, eg: $\begin{aligned} & \text { - } 35+45=90 \text { (error) } \\ & 100-90=10 \\ & 56 \div 35=1.6 \\ & 1.6 \times 10=16 \end{aligned}$ <br> - $35 \%$ of children $=56$ <br> total children $=56 \times 100 \div 35=150$ (error) <br> Reception $=100-(45+35) \%=20 \%$ <br> Reception $=20 \%$ of 150 <br> $0.2 \times 150=40$ (error) <br> - $35 \%$ is 56 <br> $5 \%$ is 8 <br> $20 \%$ is $4 \times 8=24$ (error) | $2 m$ <br> or <br> 1 m | $x$ Do not accept $160^{\circ}$ or 160\% |

## Paper 2: Calculator allowed

| Question | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| 11 | $25.7$ | 2m | ! Measures <br> See guidance (page 7) <br> Equivalent fractions or decimals, eg: <br> - $25 \frac{7}{10}$ <br> $\checkmark$ Accept 25 or 26 (an answer that has been rounded or truncated) <br> $\checkmark \quad$ For $2 m$, use of $\pi$ other than 3 or 3.14 (the given approximation), ie: <br> - 25.71 <br> - 25.7(...) <br> - 25.5 <br> - $10+5 \pi$ <br> - $25 \frac{5}{7}$ |
|  | 15.7 seen (half the perimeter of the circle, without the straight edge added) <br> OR <br> Shows or implies a complete, correct method, eg: <br> - $\frac{1}{2}(3.14 \times 10)+10$ | or 1 m | For $1 m$, use of $\pi$ other than 3 or 3.14 (the given approximation), ie: <br> - 15.71 <br> - 15.7(...) <br> - 15.5 <br> - $5 \pi$ <br> - $15 \frac{5}{7}$ |
| 12 | 11 OR 12 OR any value between 11.5 and 11.6 inclusive <br> Any value between 277 and 288 inclusive seen (value takes account of seconds in a minute and minutes in an hour) <br> OR <br> Any value between 694 and 695 inclusive seen (value takes account of hours in a day and either seconds in a minute or minutes in an hour) <br> OR <br> Shows or implies a complete, correct method, eg: <br> - $1000000 \div 60 \div 60 \div 24$ <br> - $1000000 \div 86400$ <br> - $16666 \div 60 \div 24$ | $2 m$ <br> or <br> 1m | $x$ Place value errors in the value taken for one million in an otherwise correct method, eg: <br> - $100000 \div 60 \div 60 \div 24$ |

## Standards <br> \& Testing <br> Agency

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