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KEY STAGE

3

TIER

5-7

2005

Mathematics test

Paper 2

Calculator allowed

Please read this page, but do not open your booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below.

First name _____

Last name _____

School _____

Remember

- The test is 1 hour long.
- You may use a calculator for any question in this test.
- You will need: pen, pencil, rubber, ruler, angle measurer or protractor and a scientific or graphic calculator.
- Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper – do not use any rough paper. Marks may be awarded for working.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

For marker's
use only

| | |
|------------------|--|
| Total marks | |
| Borderline check | |

QCA/05/1434

Instructions

Answers



This means write down your answer or show your working and write down your answer.

Calculators

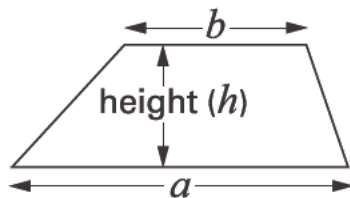


You **may** use a calculator to answer any question in this test.

Formulae

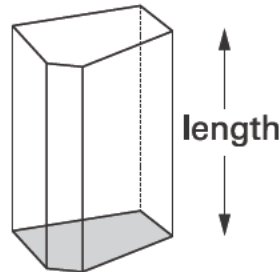
You might need to use these formulae

Trapezium



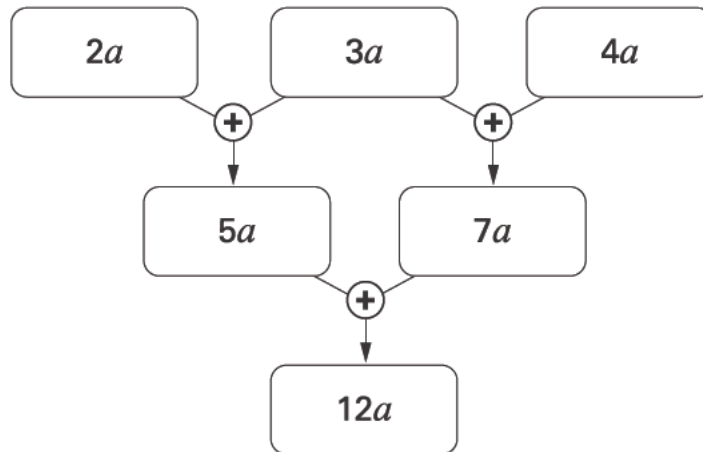
$$\text{Area} = \frac{1}{2}(a + b)h$$

Prism

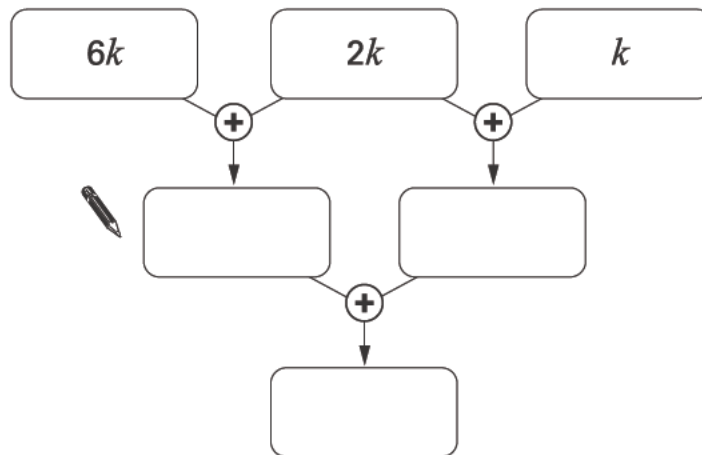


$$\text{Volume} = \text{area of cross-section} \times \text{length}$$

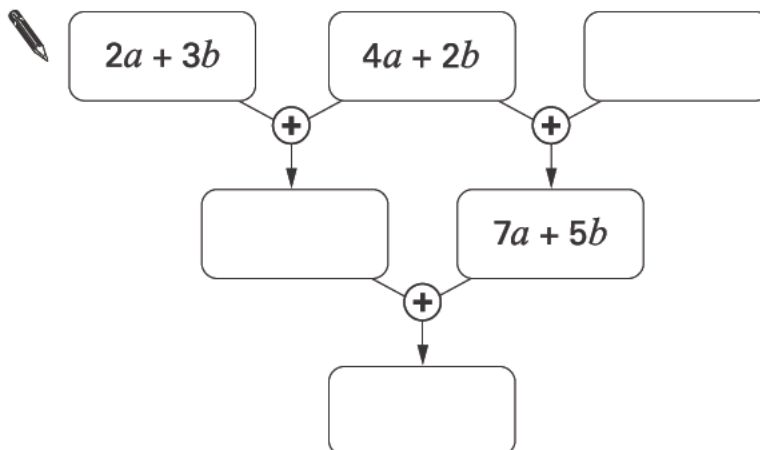
1. Look at this algebra grid.



Complete the algebra grids below, simplifying each expression.



1 mark

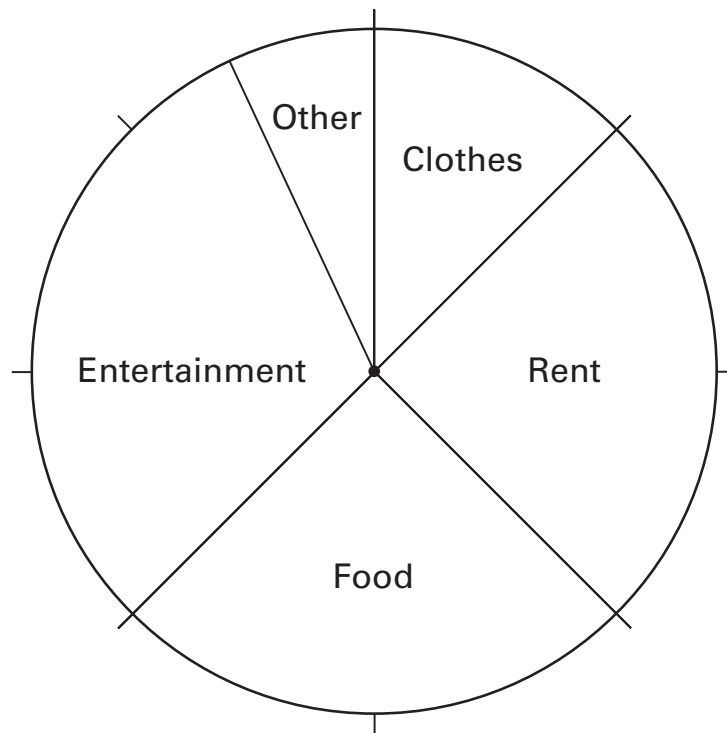


2 marks

2. Look at this information.

In 1976, a man earned £16 each week.

The pie chart shows how he spent his money.



(a) How much did the man spend on **food** each week?



£

1 mark

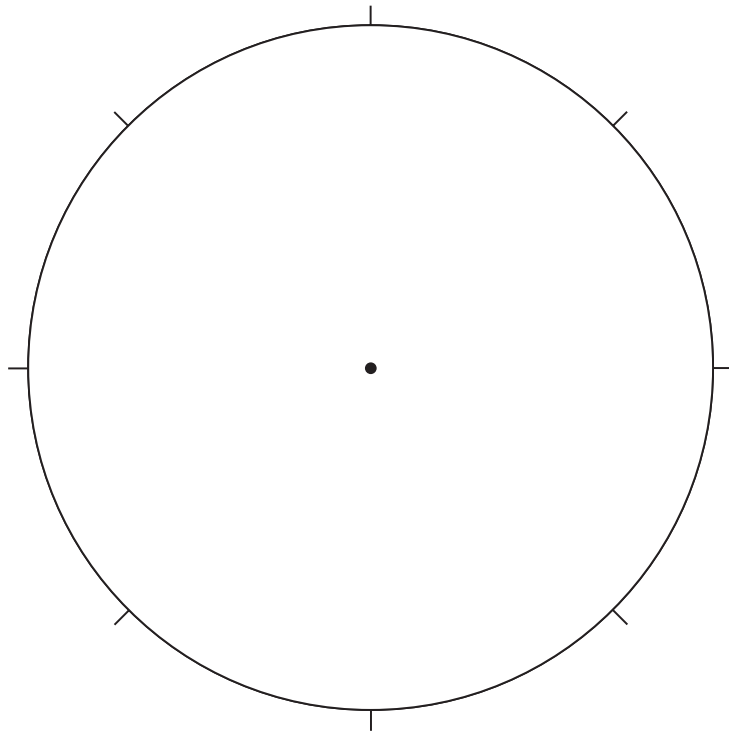
(b) Now look at this information.

In 2002, a man earned £400 each week.

The table shows how he spent his money.

| | |
|---------------|------|
| Rent | £200 |
| Food | £100 |
| Entertainment | £50 |
| Other | £50 |

Complete the pie chart below to show how the man spent his money.
Remember to **label** each sector of the pie chart.



.....
.....
2 marks



3. Two shops sell packs of pens.

| Supermarket |
|-------------------------|
| Pack of 5 pens £6.25 |

| Village shop |
|-------------------------|
| Pack of 6 pens £7.20 |

I want to buy **30 pens**.

In which shop are the pens cheaper?

You **must** show your working.



Tick (✓) your answer.

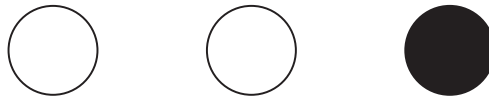


Supermarket

Village shop

.....
.....
2 marks

4. (a) Aidan puts 2 white counters and 1 black counter in a bag.



He is going to take one counter without looking.

What is the **probability** that the counter will be **black**?



.....
1 mark

- (b) Aidan puts the counter back in the bag and then puts **more black** counters in the bag.

He is going to take one counter without looking.

The **probability** that the counter will be black is now $\frac{2}{3}$

How many more black counters did Aidan put in the bag?

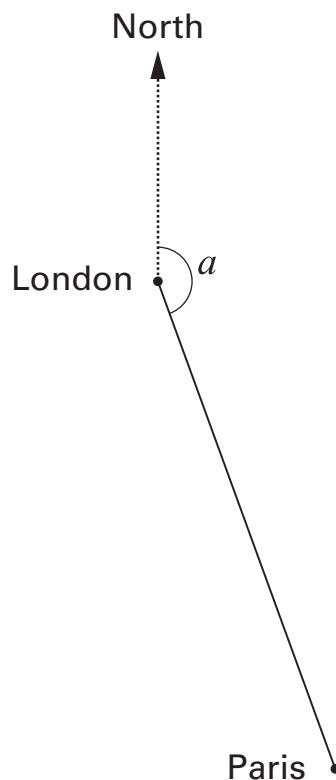


.....

.....
1 mark



5. The scale drawing shows the positions of London and Paris.



- (a) From London to Paris, the angle from north is angle a
Measure accurately angle a



$a = \dots\dots\dots^\circ$

$\dots\dots\dots$
1 mark

- (b) On the scale drawing, **1 cm represents 50 km.**

What is the distance, in km, from London to Paris?



$\dots\dots\dots$ km

$\dots\dots\dots$
1 mark

(c) A newspaper printed this information about London and Madrid.

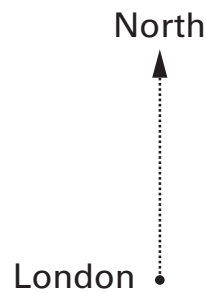
From London to Madrid, the angle from north is **195° clockwise**.

Madrid is **1300 km** from London.

Show this information on a scale drawing.

Use the scale **1 cm represents 200 km**.

The position of London is shown for you.



.....
.....
2 marks



6. Work out the number of boys and girls in each class below.

(a) In class 8M, there are **27 pupils**.

There are **twice as many boys** as girls.



| Number of boys | Number of girls |
|----------------|-----------------|
| | |

.....
1 mark

(b) In class 8K, there are **28 pupils**.

There are **two more boys** than girls.



| Number of boys | Number of girls |
|----------------|-----------------|
| | |

.....
1 mark

(c) In class 8T, there are **9 boys**.

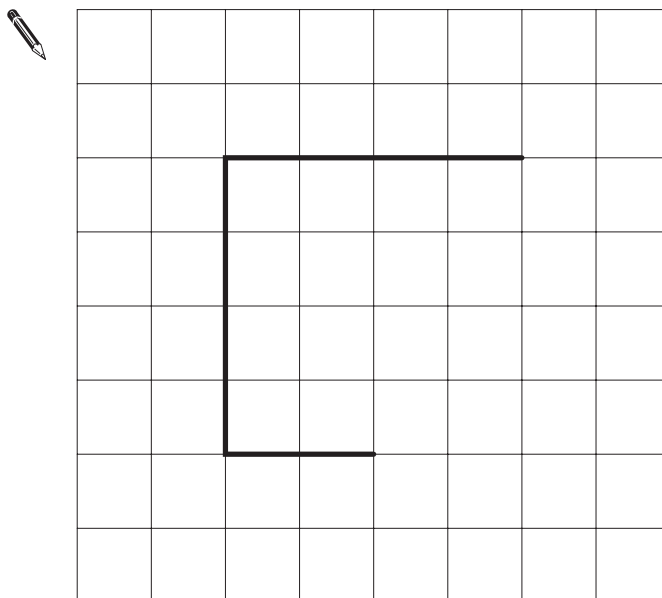
The ratio of boys to girls is **1 : 2**



| Number of boys | Number of girls |
|----------------|-----------------|
| | |


.....
1 mark

7. Here are three lines on a centimetre square grid.
 Draw two more lines on the grid to make a **pentagon** that has an **area of 14 cm²**



.....
1 mark

8. Use your calculator to work out the answers.

 $(48 + 57) \times (61 - 19) = \dots\dots\dots$

.....
1 mark

$$\frac{48 + 57}{61 - 19} = \dots\dots\dots$$

.....
1 mark



9. Each year, there is a tennis competition in Australia and another one in France.

The table shows how much money was paid to the winner of the men's competition in each country in 2002.

| Country | Money |
|-----------|--|
| Australia | 1 000 000 Australian dollars (£1 = 2.70 Australian dollars) |
| France | 780 000 Euros (£1 = 1.54 Euros) |

Which country paid **more** money?

You **must** show your working.



Tick (✓) the country that paid more.



Australia

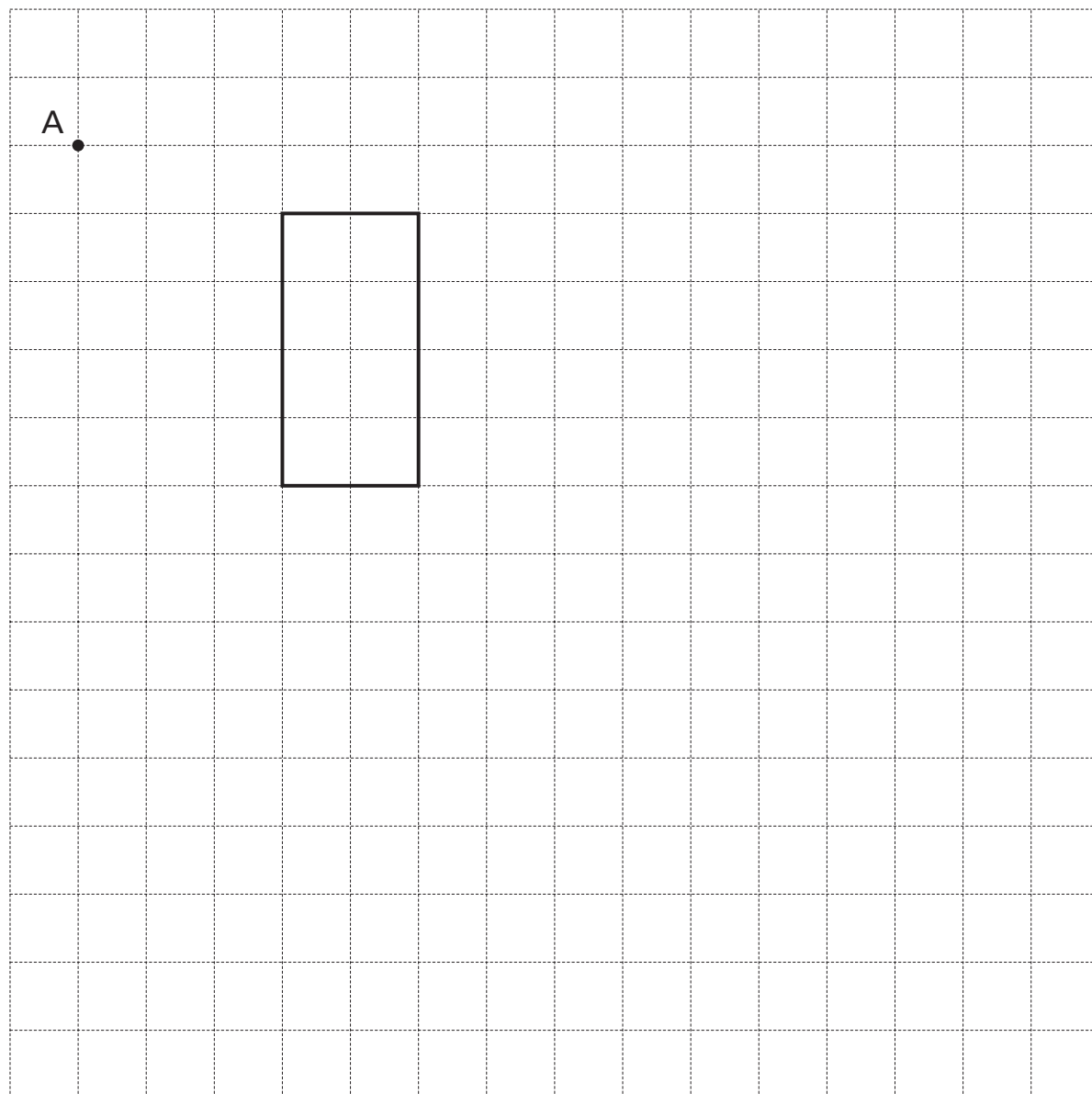
France

.....
.....
2 marks

10. Look at the rectangle drawn on a square grid.

Draw an **enlargement** of this rectangle with **scale factor 2**

Use **point A** as the **centre** of enlargement.



.....
.....
2 marks

11. About 2000 years ago, a Greek mathematician worked out this formula to find the area of any triangle.

For a triangle with sides a , b and c

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{where } s = \frac{a+b+c}{2}$$

A triangle has sides, in cm, of 3, 5 and 6

Use $a = 3$, $b = 5$ and $c = 6$ to work out the area of this triangle.



cm²

.....
.....
2 marks

12. Here is some information about all the pupils in class 9A.

| | girls | boys |
|--------------|-------|------|
| right-handed | 13 | 14 |
| left-handed | 1 | 2 |

A teacher is going to choose a pupil from 9A at random.

- (a) What is the probability that the pupil chosen will be a **girl**?



1 mark

- (b) What is the probability that the pupil chosen will be **left-handed**?



1 mark

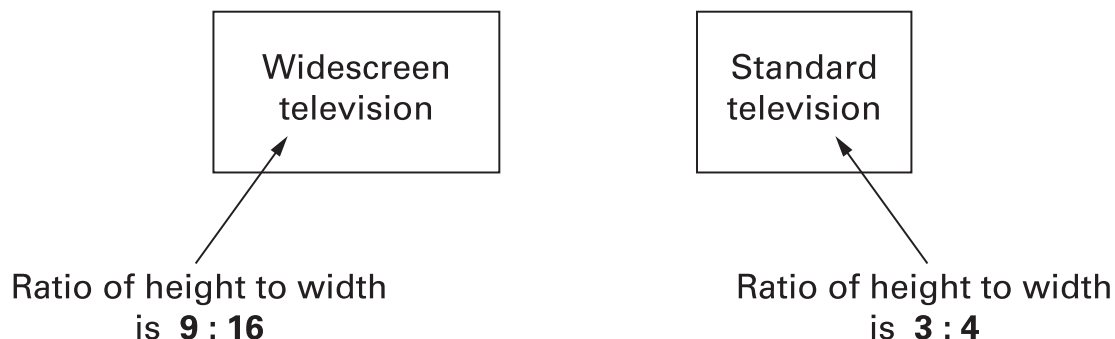
- (c) The teacher chooses the pupil at random.
She tells the class the pupil is **left-handed**.

What is the probability that this left-handed pupil is a **boy**?



1 mark

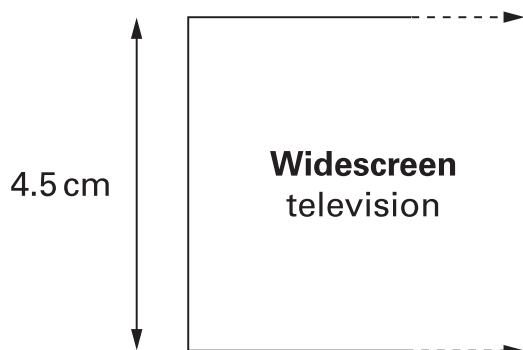
13. The screens of widescreen and standard televisions look different. They have different proportions.



Keri starts to draw scale drawings of the televisions.

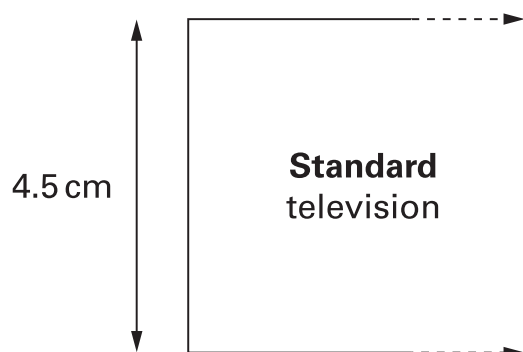
For each, the height is 4.5 cm.

What should the **width** of each scale drawing be?



The width of this scale drawing
should be cm

.....
1 mark



The width of this scale drawing
should be cm

.....
1 mark

14. A spinner has the numbers 1 to 4 on it.

The probability of spinning a number 4 is 0.1

The probability of spinning a number 1 is 0.6

The probability of spinning a number 2 is the same as
the probability of spinning a number 3

Calculate the probability of spinning a **number 3**



.....
.....
2 marks

15. I think of a number.

I multiply this number by **8**, then subtract **66**

The result is twice the number that I was thinking of.

What is the number I was thinking of?



.....
.....
2 marks



16. Here is some information about A levels in 2002.

| | English | Mathematics |
|----------------------------|---------|-------------|
| Number of students | 72 000 | 54 000 |
| Percentage gaining grade A | 19% | 37% |

How many more students gained grade A in mathematics than in English?



.....
.....
2 marks

17. (a) Look at this equation.

$$14y - 51 = 187 + 4y$$

Is $y = 17$ the solution to the equation?



Yes

No

Show how you know.



1 mark

(b) Now look at this equation.

$$3y^2 = 2601$$

Is $y = 17$ a solution to the equation?



Yes

No

Show how you know.



1 mark

18. Write these expressions as simply as possible.



$$9 - 3k + 5k = \dots\dots\dots$$

1 mark

$$k^2 + 2k + 4k = \dots\dots\dots$$

1 mark

$$3k \times 2k = \dots\dots\dots$$

1 mark

$$\frac{9k^2}{3k} = \dots\dots\dots$$

1 mark

19. In one week Jamal watched television for **26 hours**.

In that week:

He watched television for the **same** length of time on Monday, Tuesday, Wednesday and Thursday.

On each of Friday, Saturday and Sunday, he watched television for **twice as long** as on Monday.

How long did he spend watching television on **Saturday**?

Write your answer in hours and minutes.



..... hours minutes

.....
.....
2 marks



20. Here are four charts drawn by a computer.

**Charts to show the average amount of milk
produced by different breeds of cow**

Chart 1

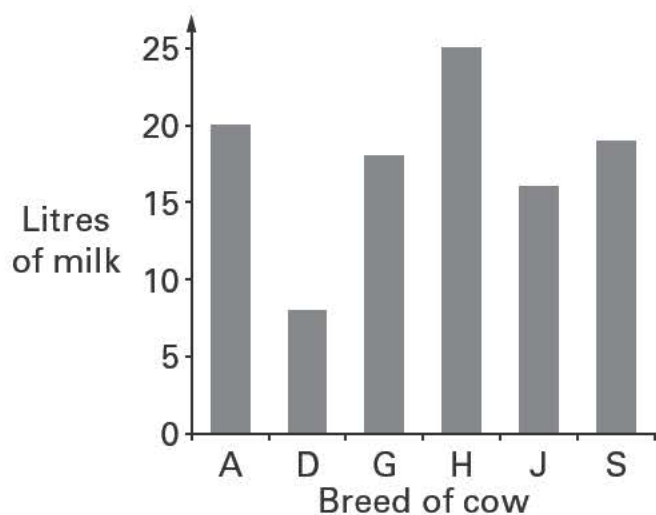


Chart 2

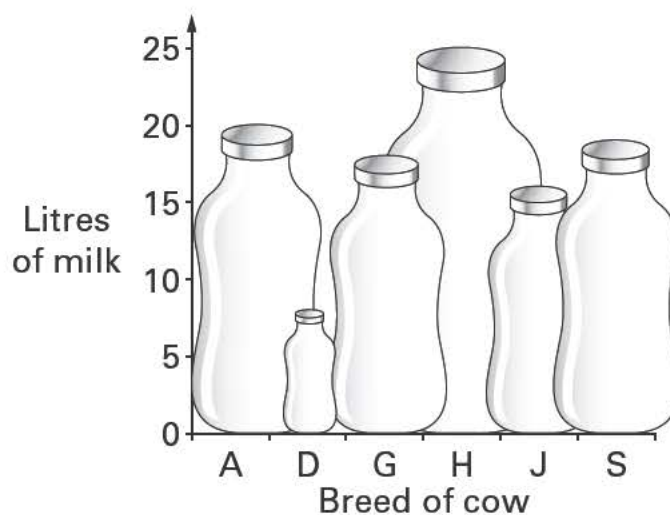


Chart 3

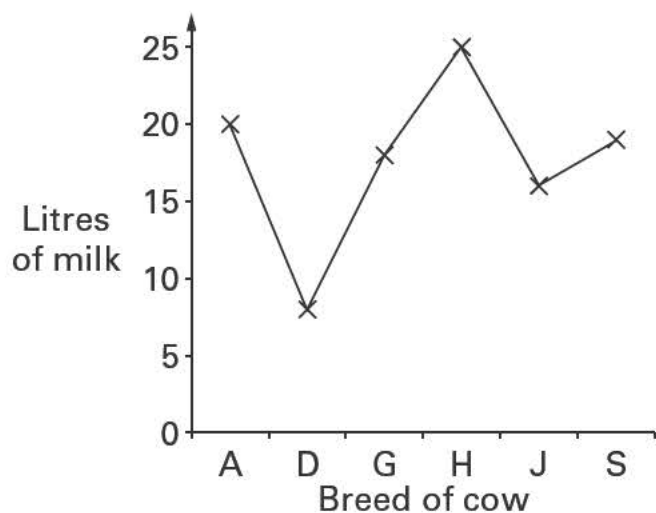
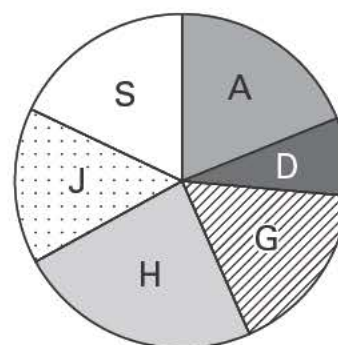


Chart 4



Key:

A - Ayrshire D - Dexter G - Guernsey H - Holstein J - Jersey S - Shorthorn

Only one of these charts is a good way of showing the data.

For each of the other three charts, explain why the type of chart is **not** a good way of showing the data.



Chart

because

.....

.....

.....
1 mark

Chart

because

.....

.....

.....
1 mark

Chart

because

.....

.....

.....
1 mark



21. (a) The n th term of a sequence is $3n + 4$

What is the **8th** term of this sequence?



.....

.....
1 mark

(b) The n th term of a different sequence is $\frac{n - 2}{n^2}$

Write the first **three** terms of this sequence.



.....

.....
2 marks

22. Multiply out the brackets in these expressions.



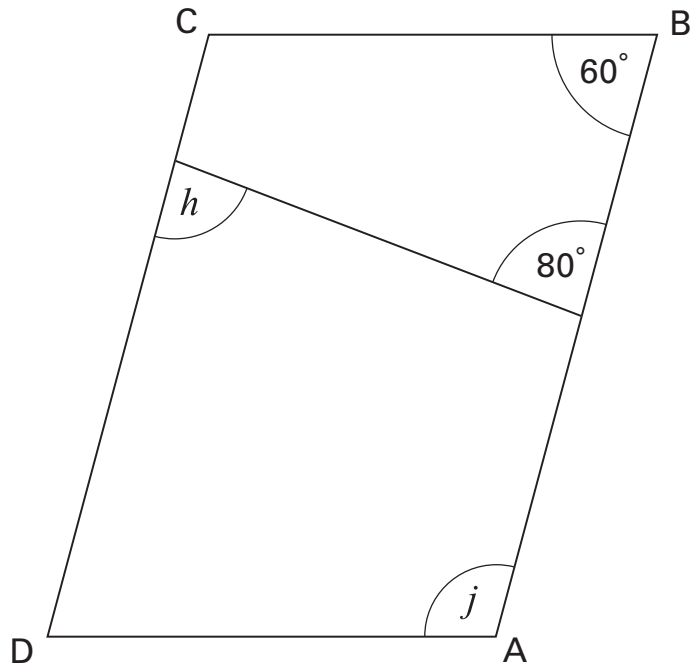
$$y(y - 6) = \dots\dots\dots$$

.....
1 mark

$$(k + 2)(k + 3) = \dots\dots\dots$$

.....
1 mark

23. ABCD is a parallelogram.



Not drawn accurately

Work out the sizes of angles h and j

Give reasons for your answers.



$h = \dots\dots\dots^\circ$ because

.....

.....

.....

1 mark

$j = \dots\dots\dots^\circ$ because

.....

.....

.....

1 mark



24. A newspaper printed this information about the world's population.

If the world was a village of 100 people,
6 people would have **59%** of the total wealth.
The other 94 people would have the rest.

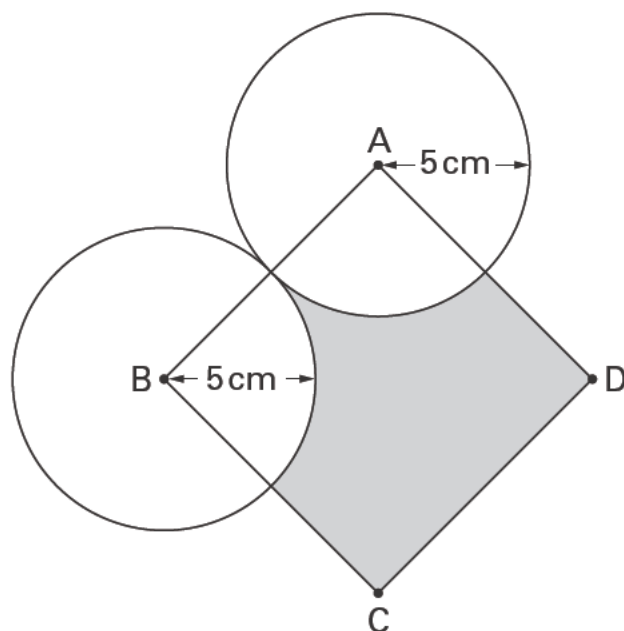
On average, **how many times** as wealthy as one of the other 94 people would one of these 6 people be?



.....
.....

2 marks

25. The diagram shows two circles and a square, ABCD.
 A and B are the centres of the circles.
 The radius of each circle is **5 cm**.



Not drawn
accurately

Calculate the area of the **shaded part** of the square.



.....

.....

.....
2 marks

.....
1 mark



END OF TEST